Collaborative Project

GeoKnow - Making the Web an Exploratory for Geospatial Knowledge

Project Number: 318159 **Start Date of Project:** 2012/12/01 **Duration:** 36 months

Deliverable 3.4.1
Metrics for Linked Geospatial Information

Dissemination Level	Public
Due Date of Deliverable	Month 18, 31/05/2014
Actual Submission Date	Month 19, 30/06/2014
Work Package	WP3
Task	T3.4
Type	Report
Approval Status	Final
Version	1.0
Number of Pages	23
Filename	D3.4.1_Metrics_for_linked_geospatialinformation.pdf

Abstract: This report presents the initial development around enabling measurable statistics of maps such as coverage, level of detail, precision and degree of annotation with metadata.

Project funded by the European Commission within the Seventh Framework Programme (2007 - 2013)

History

Version	Date	Reason	Revised by
0.1	01/03/2014	Provide initial draft of this document for internal contributions	Mohamed Sherif, Axel-Cyrille Ngonga Ngomo
0.2	29/05/2014	First final version of the document	Axel-Cyrille Ngonga Ngomo
0.3	31/05/2014	Feedback	Giorgos Giannopoulos
0.3	20/06/2014	Review	Matthias Wauer
0.4	26/06/2014	Final version of the document	Axel-Cyrille Ngonga Ngomo

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Executive Summary

Community-provided information can surpass the level of detail found in official and commercial maps. To compare these datasets with reference datasets, metrics for linking the resources in the datasets are central to derive statistics that allow comparing the level of detail of the same data items as well as the density of data items in the different datasets. For example, the precision and the recall achieved by a crowd-sourced dataset can only be computed if equivalent resources can be linked across different datasets. In this deliverable, we thus survey and evaluate measures for comparing these geometries w.r.t. to the two main types of differences that can occur across datasets, i.e., difference in granularity and measurement. We show that the mean distance is both the most scalable and in the many cases the most reliable measure for linking resources across different geo-spatial knowledge bases. Preliminary experiments with ORCHID yet suggest that almost all measures are amenable to scale even on large datasets. In the second version of this deliverable, we will combine these links with SPARQL queries to provide a full comparison of crowd-sourced datasets with reference data.

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1 Introduction

The Web of Data has grown significantly over the last years. In particular, very large geo-spatial datasets such as LinkedGeoData (LGD) with 20+ billion triples [4] have been made available. Interestingly, community-provided information such as LinkedGeoData can surpass the level of detail found in official and commercial maps. To compare these datasets with reference datasets, it is central to derive statistics that allow comparing the level of detail of the same data items as well as the density of data items in the different datasets. A survey of papers and standards on data quality for geo-spatial data[1] suggests three major approaches to compare geo-spatial datasets:

1. *Completeness*: Completeness can describe two things: First, this measure stands for the number of object from the reference datasets that can be found in the contributed datasets. This aspect of completeness is called *coverage* in the description of work. From an information retrieval point of view, it is akin to the recall. However, the precision can be computed directly from the same data. In literature, the term completeness can also stand for the number of geo-spatial features to describe the same real-world object across different datasets. This aspect of completeness (which is equivalent to the *degree of annotation with metadata* in the description of work) can be computed easily using SPARQL queries and will not be covered in this deliverable.

2. *Positional accuracy*: This criterion stands for how well the location of real-world objects is described in the crowd-sourced dataset in comparison to the reference dataset. Measuring this criterion demands the definition of a notion of distance between vector geometries. Once this notion has been defined, this measure pertains to the distance between the vector geometries that represent the same real-world objects across the community-provided and the reference dataset. Interestingly, distance measures that are not robust against errors are most appropriate to quantify this criterion.

3. *Resolution*: This criterion measures the degree of accuracy of the measurement for single points of the vector geometries, i.e., the standard deviation of the measurements of points that are elements of the vector geometry which describes the same real-world objects. It is also used to describe the difference in the number of points that were used to describe the geometries of the same real-world objects across the datasets. This last aspect of resolution (also dubbed granularity) was dubbed *level of detail* in the description of work.

Other metrics described in T3.4 can be derived directly from SPARQL queries to a triple store that supports geo-spatial queries. For example, the *coverage and pertinence of a category in a region* would simply count the number of instances of the category within the polygon that describes the region. The *timeliness* can be computed by querying for the data at which an item was added to the data.

In all cases, knowing which resources from the reference datasets are described in the community-provided dataset is of central importance to compute these measures. With respect to the completeness of the datasets, the links between the two datasets allow to measure the precision and the recall achieved by the crowd-sourced dataset. Similarly, the positional accuracy and the resolution of a dataset can also be measured if the resources have been disambiguated. In this first version of this deliverable, we thus survey and evaluate measures for comparing the vector geometries that describe geo-spatial resources w.r.t. two main types of differences that can occur across datasets, i.e., difference in granularity (resolution) and measurement (accuracy). A measure for the completeness of a dataset can be derived from linking geo-spatial resources across the different datasets. We show that the mean distance is both the most scalable and in the many cases the most reliable measure for linking resources across different geo-spatial knowledge bases.

[1] All details of the survey will be presented in D3.5.1.

Preliminary experiments with ORCHID yet suggest that almost all measures are amenable to scale even on large datasets. Moreover, our results also suggest that the Fréchet distance is most sensitive to errors in datasets. In the second version of this deliverable, we will use these insights to provide algorithms to measure these three main criteria at different levels of administration granularity (city, county, province, state, etc.).

The remainder of this report is structured as follows: Section 2 exemplifies the types of errors that can occur when representing the geometry of the same real-world geo-spatial object across different datasets. Section 3 introduces some basic assumption and notations that will be used all over the rest of the report. Then, in Section 4 we give a detailed description of each point set distance functions, as well as their mathematical formulation and different implementations. Thereafter, in Section 5 we present an evaluation of our work w.r.t. both scalability and robustness. Finally, we conclude the report with a brief overview of related work (Section 6), as well as a conclusion and future work (Section 7). All measures and algorithms presented herein were integrated into the LIMES framework.[2]

[2] http://limes.sf.net

2 Discrepancies and Measurements

Most of the existing solutions to linking (see [5, 21] for an overview) address this problem by using a complex similarity or distance function to compare instances from two (not necessarily distinct) knowledge bases. The result of the function is then compared to a threshold. The result of the comparison is finally used to suggest the existence of a link between instances. While previous works have compared a large number of measures with respect to how well they perform in the link discovery task [9], measures for linking geo-spatial resources have been paid little attention to. Previous works have yet shown that domain-specific measures and algorithms are required to tackle the problem of geo-spatial link discovery [22]. For example, 20,354 pairs of cities in DBpedia share exactly the same label. For villages in LinkedGeoData, this number grows to 3,946,750. Consequently, finding links between geo-spatial resources requires devising means to distinguish them using their geo-spatial location. On the Web of Data, the geo-spatial location of resources is most commonly described using either points or more generally by means of vector geometry. Thus, devising means for using geo-spatial information to improve link discovery requires providing means to measure distances between such vector geometry data.

Examples of vector geometry descriptions for the country of Malta are shown in Figure 1. As displayed in the examples, two types of discrepancies occur when one compares the vector descriptions of the same real-world entity (e.g., Malta) in different datasets: First, the different vector descriptions of a given real-world entity often comprise different points across different datasets. For example, Malta's vector description in DBpedia contains the point with latitude 14.46 and longitude 35.89. In LGD, the same country is described by the point of latitude 14.5 and longitude 35.9. We dub the discrepancy in position (latitude and longitude) for points in the vector description *measurement discrepancy*. A second type of discrepancy that occurs in the vector description of geo-spatial resources across different datasets are discrepancies in *granularity* (also dubbed resolution). For example, Malta is described by one polygon in DBpedia , two polygons in Nuts and a single point in LGD.

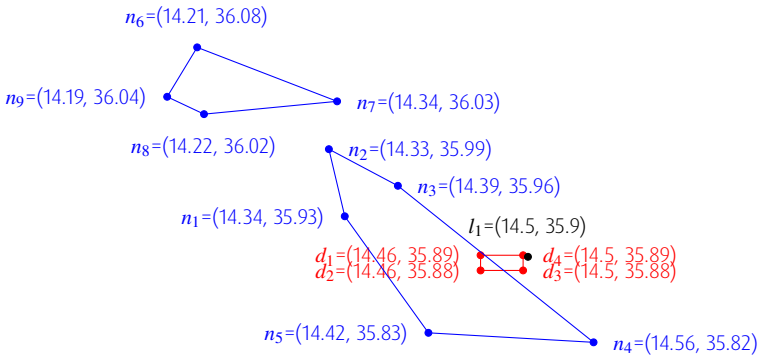


Figure 1: Vector description of the country of *Malta*. The blue polygons shows the vector geometry for *Malta* in the *Nuts* dataset, the red polygon shows the same for the *DBpedia*, while the black point shows the location of the same real-world entity according to *LinkedGeoData*.

Analysing the behaviour of different measures with respect to these two types of discrepancies is central to detect the measures that should be used for geo-spatial link discovery. Moreover, such an analysis also allows to elucidate which measures should be used to compute the completeness, positional accuracy and resolution of a community-generated geo-spatial dataset. In this report, we address these research gaps by first surveying existing measures that can be used for comparing vector descriptions. We then compare these measures in series of experiments on samples extracted from three real datasets with the aim of answering the following questions:

Q_1: Which of the existing measures is the most time-efficient measure?

Q_2: Which measure generates mappings with a high precision, recall, or F-measure?

Q_3: How well do the measures perform when the datasets have different granularities?

Q_4: How sensitive are the measures to measurement discrepancies?

Q_5: How robust are the measures when both types of discrepancy occur?

3 Preliminaries and Notation

We assume the link discovery problem as being formulated in a way akin to [22]: Given two sets S and T of resources as well as a predicate p, compute the set $M = \{(s,t) \in S \times T :< s,p,t > holds\}$, where $< s,p,t >$ is the RDF triple with the subject s, the predicate p and the object t. Computing M directly is commonly a non-trivial task. State-of-the-art link discovery systems thus most commonly aim to compute an approximation M' of M with $M' = \{(s,t) : \delta(s,t) \leq \theta\}$, where δ is a complex distance function and θ is a distance threshold. δ most commonly consists of a combination of atomic measures which can be used to compare property values of the resources s and t. For example, the edit distance is an atomic measure that can be used to compare the labels of two resources.

In addition to bearing properties similar to those bared by other types of resources (label, country, etc.), geo-spatial resources are commonly described by means of vector geometry.[3] Each vector description can be modelled as a set of points. We will write $s = (s_1, \ldots, s_n)$ to denote that the vector description of the resource s comprises the points $s_1, \ldots, s_n$. A point s_i on the surface of the planet is fully described by two values: its latitude $lat(s_i) = \varphi_i$ and its longitude $lon(s_i) = \lambda_i$. We will denote points s_i as pairs (φ_i, λ_i). Then, the distance between two points s_1 and s_2 can be computed by using the *orthodromic distance* $\delta(s_1, s_2) = R \cos^{-1}(\sin(\varphi_1)\sin(\varphi_2) + \cos(\varphi_1)\cos(\varphi_2)\cos(\lambda_2 - \lambda_1))$, where $R = 6371km$ is the planet's radius.[4] Computing the distance between sets of points is yet a more difficult endeavour. Over the last years, several measures have been developed to achieve this task. Most of these approaches regard vector descriptions as ordered set of points. In the following sections, we present such measures and evaluate their robustness against different types of discrepancies.

[3] Most commonly encoded in the WKT format, see http://www.opengeospatial.org/standards/sfa.
[4] We assume the planet to be a perfect sphere.

4 Distance Measures for Point Sets

We carried out a systematic study of the literature on distances for point sets according to the approach presented in [18, 20]. The systematic survey results were retrieved from seven different scientific search engines[5]. The search engines returned 19869 distinct publications. We then excluded publications that were not in English or did not discuss algorithms for finding distances between vector geometries. Moreover, we excluded all publications that were not peer-reviewed as well as works that were published as posters or abstracts. Overall, 21 publications were deemed relevant and contained measures that could used to compare point sets. We discarded those measures that are only relevant for convex polygons given that this condition does not necessarily hold for the descriptions of geo-spatial entities. Overall, 10 different distances for point sets could be retrieved from the relevant publications. In the following, we present each of these distances and exemplify it by using the DBpedia and Nuts descriptions of Malta presented in Figure 1. The input for the distances consists of two point sets $s = (s_1, \ldots, s_n)$ and $t = (t_1, \ldots, t_m)$, where n resp. m stands for the number of distinct points in the description of s resp. t. W.l.o.g, we assume $n \geq m$.

4.1 Mean Distance Function

The mean distance is one of the most efficient distance measures for point sets. First, a mean point is computed for each point set. Then, the distance between the two means is computed by using the orthodromic distance. Formally: $D_{mean}(s,t) = \delta\left(\frac{\sum_{s_i \in S} s_i}{n}, \frac{\sum_{t_j \in T} t_j}{m}\right)$. D_{mean} can be computed in $O(n)$. For our example, the mean of the DBpedia description of Malta is the point (14.48, 35.89). The mean for the Nuts description are (14.33, 35.97). Thus, D_{mean} returns $18.46km$ as the distance between the two means points.

4.2 Max Distance Function

The idea behind this measure is to compute the overall maximal distance between points s_i and t_j. Formally, the maximum distance is defined as: $D_{max}(S,T) = \max_{s_i \in S, t_j \in T} \delta(s_i, t_j)$. For our example, D_{max} returns $38.59km$ as the distance between the points d_3 and n_6. Due to its construction, this distance is particularly sensitive to outliers. While the naive implementation of *Max* is in $O(n^2)$, [7] introduced an efficient implementation that achieves a complexity of $O(n \log n)$.

4.3 Min Distance Function

The main idea of the *Min* is akin to that of *Max* and is formally defined as $D_{min}(s,t) = \min_{s_i \in S, t_j \in T} \delta(s_i, t_j)$. Going back to our example, D_{min} returns $7.82km$ as the distance between the points d_2 and n_5. Like D_{max}, D_{min} can be implemented to achieve a complexity of $O(n \log n)$ [30, 19].

4.4 Average Distance Function

For computing the *average* point sets distance function, the orthodromic distances between all the source-target points pairs is cumulated and divided by the number of point source-target point pairs: $D_{avg}(s,t) =$

[5] Google Scholar, ACM Digital Library, Springer Link, Science Direct, ISI Web of Science, Semantic Web Journal, Journal of Web Semantics and Journal of Data and Knowledge Engineering.

$\frac{1}{nm}\sum_{s_i \in S, t_j \in T} \delta(s_i, t_j)$. For our example, D_{avg} returns $22km$. A naive implementation of the *average* distance is $O(n^2)$, but it can be efficiently computed in $O(n \log n)$.

4.5 Sum of Minimums Distance Function

This distance function was first proposed by [23] and is computed as follows: First, the closest point t_j to each point s_i is to be detected, i.e., the point $t_j = \arg\min_{t_k \in t} \delta(s_i, t_k)$. The same operation is carried out with source and target reversed. Finally, the average of the two values is then the distance value. Formally, the *sum of min* distance is defined as: $D_{som}(S,T) = \frac{1}{2}\left(\sum_{s_i \in S} \min_{t_j \in T} \delta(s_i, t_j) + \sum_{t_i \in T} \min_{s_j \in S} \delta(t_i, s_j)\right)$. Going back again to our example, the sum of minimum distances from each of DBpedia points describing Malta to the ones of Nuts is $37.27km$, and from Nuts to DBpedia is $178.58km$. Consequently, D_{som} returns $107.92km$ as the average of the two values. The *sum of minimum* has the same complexity as D_{min}.

4.6 Surjection Distance Function

The *surjection* distance function introduced by [25] defines the distance between two point sets as follows: The minimum distance between the sum of distances of the surjection of the larger set to the smaller one. Formally, the *Surjection* distance is defined as: $D_s(S,T) = \min_{\eta} \sum_{(e1,e2)\in\eta} \delta(e_1, e_2)$, where η is the surjection from the larger of the point sets S and T to the smaller set of points. In to our example, $\eta = (n_1, d_4)$, (n_2, d_1), (n_3, d_2), (n_4, d_3), (n_5, d_4), (n_6, d_1), (n_7, d_1), (n_8, d_1) and (n_9, d_1). Then, D_s returns $184.74km$ as the sum of the orthodromic distances between each of the point pairs included in η. A main drawback of the *surjection* is being biased toward some points ignoring some others in calculations. (i.e. putting more weight in some points more than the others) For instance in our example, η contains 5 different points surjected to d_1, while only one point surjected to d_2.

4.7 Fair Surjection Distance Function

In order to fix the biased drawback of *surjection*, [25] introduces an extension of the surjection distance which is dubbed *fair surjection*. The surjection between sets S and T is said to be *fair* if η' maps elements of S as evenly as possible to T.

The *fair surjection* is defined formally as: $D_{fs}(S,T) = \min_{\eta'} \sum_{(e1,e2)\in\eta'} \delta(e_1, e_2)$, where η' is the evenly mapped surjection from the larger of the sets S and T to the smaller. For our example, $\eta' = (n_1, d_1)$, (n_2, d_2), (n_3, d_3), (n_4, d_4), (n_5, d_1), (n_6, d_2), (n_7, d_3), (n_8, d_4) and (n_9, d_1). Then, D_{fs} returns $137.43km$ as the sum of the orthodromic distances between each of the point pairs included in η'.

4.8 Link Distance Function

The link distance introduced by [11] defines the distance between two point sets S and T as a relation $R \subseteq S \times T$ satisfying

1. For all $s_i \in S$ there exists $t_j \in T$ such that $(s_i, t_j) \in R$
2. For all $t_j \in T$ there exists $s_i \in S$ such that $(s_i, t_j) \in R$

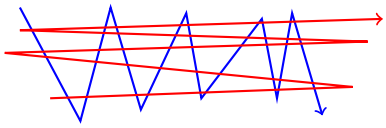


Figure 2: Fréchet vs other distance approaches

Formally, The *minimum link distance* $D_l(S,T)$ between two polygons S and T is defined by $D_l(S,T) = \min_R \sum_{(s_i,t_j)\in R} \delta(s_i,t_j)$, where minimum is computed from all relations R, where R is a linking between S and T satisfying the previous two conditions. For our example, the small granularity of the Malta descriptions in the datasets at hand leads to D_l having the same results as D_{fs}. See [11] for an analysis of the complexity of the *surjection*, *fair surjection* and *link* distance functions.

4.9 Hausdorff Distance Function

The *Hausdorff* distance is a measure of the maximum of the minimum distances between two sets of points. Hausdorff is one of the commonly used approach for determining the similarity between point sets [16]. Formally, the Hausdorff distance is defined as $D_h(S,T) = \max_{s_i\in S}\{\min_{t_j\in T}\{\delta(s_i,t_j)\}\}$. In our example, the algorithm finds the orthodromic distance between each of the points of DBpedia to the nearest point of Nuts, which is computed to be the distance between the point pairs (d_1,n_5), (d_2,n_5), (d_3,n_4), and (d_4,n_4). Then, D_h is the maximum distance of them, which is between the point d_4 and n_4 equals $34.21km$. [22] introduces two efficient approaches for computing bound Hausdorff distance.

4.10 Fréchet Distance Function

Most of the distances presented before have a considerable common disadvantage. Consider the two curves shown in Figure 2, Any point on one of the curves has a nearby point on the other curve. Therefore, many of the measures presented so far (incl. Hausdorff, min, sum of mins) return a low distance. However, these curves are intuitively quite dissimilar: While they are close on a point-wise basis, they are not so close if we try to map the curves continuously to each other. A distance measure that captures this intuition is the *Fréchet* [14] distance.

The basic idea behind the Fréchet distance is encapsulated in the following example[6]: *Imagine two formula one racing cars. The first car, A, hurtles over a curve formulated by a first point set. The second car does the same over a curve formulated by the second point set. The first and second car will vary in velocity but they do not move backwards over their curves. Then the Fréchet distance between the point sets is the minimum length of a non-stretchable cable that would be attached to both cars and would not break during the race.*

In order to drive a formal definition of Fréchet distance, First we define *A curve* as a continuous mapping $f : [a,b] \to V$ with $a,b \in \mathbb{R}$, and $a < b$, where *V denote an arbitrary vector space*. A polygonal curve is $P : [0,n] \to V$ with $n \in \mathbb{N}$, such that for all $i \in \{0,1,...,n-1\}$ each $P[i,i+1]$ is *affine*, i.e. $P(i+\lambda) = (1-\lambda)P(i) + \lambda P(i+1)$ for all $\lambda \in [0,1]$. n is called the length of P.

Then, Formally, Fréchet distance can be defined as:

$$D_f(S,T) = \inf_{\substack{\alpha[0,1]\to[s_1,s_n] \\ \beta[0,1]\to[t_1,t_n]}} \left\{ \sup_{t\in[0,1]} \left\{ \delta(f(\alpha(t)) - g(\beta(t))) \right\} \right\} \quad (1)$$

[6] Adapted from [1].

where $f : [s_1, s_n] \rightarrow V$ and $g : [t_1, t_n] \rightarrow V$. α, β range over continuous and increasing functions with $\alpha(0) = s_1$, $\alpha(1) = s_n$, $\beta(0) = t_1$ and $\beta(1) = t_n$ only. Computing the Fréchet distance for our example returns $0.3km$. See [2] for an analysis of the complexity of the Fréchet distance. Overall, the distance measures presented above return partly very different values ranging from $0.3km$ to $184.74km$ even on our small example. In the following, we evaluate how well these measures can be used for link discovery.

5 Evaluation

The goal of our evaluation was to answer the five questions mentioned in Section 1. To this end, we devised three series of experiments. First, we evaluated the scalability of the ten measures with growing dataset sizes. Then, we measured the robustness of these measures against measurement and granularity discrepancies as well as combinations of both. Finally, we measured the scalability of the measures when combined with the ORCHID algorithm.

5.1 Experimental Setup

5.1.1 Datasets

We used three publicly available datasets for our experiments. The first dataset, *Nuts*[7] was used as core dataset for our scalability experiments. We chose this dataset because it contains fine-granular descriptions of 1,461 geo-spatial resources located in Europe. For example, Norway is described by 1981 points. The second dataset, *DBpedia*[8], contains all the 731,922 entries from DBpedia that possess geometry entries. We chose DBpedia because it is commonly used in the Semantic Web community. Finally, the third dataset, *LGD*, contains all 3,836,119 geo-spatial objects from http://linkgeodata.org that are instances of the class Way.[9] Further details to the datasets can be found in [22].

5.1.2 Benchmark

To the best of our knowledge, there is no established gold standard benchmark geographic dataset that can be used to evaluate the robustness of geo-spatial distance measures. We thus adapted the benchmark generation approach proposed by [13] to geo-spatial distance measures. We implemented two modifiers, which both take a polygon s and a threshold as input and return a polygon. The *granularity modifier* M_g regards the threshold $\gamma \in [0, 1]$ as the probability that a point of s will be in the output polygon. To ensure that an empty polygon is never generated, the modifier always includes the first point of s into its output. For all other points s_i, a random number r between 0 and 1 is generated. If $r \leq \gamma$, then s_i is added to the output of the modifier. Else, s_i is discarded. The *measurement error modifier* M_e emulates measurement errors across datasets. To this end, it alters the latitude and longitude of each the points of s by at most the threshold μ. Consequently, the new coordinates of a point s_i are located within a square of size 2μ with s_i at the center. We used a sample of 200 points from each dataset for our discrepancy experiments.

To measure how well each of the distances performed w.r.t. to the modifiers, we first created a reference mapping $M = \{(s, s) \in S\}$ when given a set of input resources S. Then, we applied the modifier to all the elements of S to generate a target dataset T. We then measured the distance between each of the point sets in the set T and the resources in S. For each element of S we stored the closest point $t \in T$ in a mapping M'. We now computed the precision, recall and F-measure achieved within the experiment by comparing the pairs in M' with those in M.

[7] Version 0.91 available at http://nuts.geovocab.org/data/ is used in this work
[8] We used version 3.8 as available at http://dbpedia.org/Datasets.
[9] We used the RelevantWays dataset (version of April 26th, 2011) of *LinkedGeoData* as available at http://linkedgeodata.org/Datasets.

5.1.3 Hardware

All experiments were carried out on a 64-core server running *OpenJDK* 64-Bit Server 1.6.0_27 on *Ubuntu* 12.04.2 LTS. The processors were 12 Hexa-core *AMD Opteron* 6128 clocked at 2.0 GHz. Unless stated otherwise, each experiment was assigned 8 GB of memory and was ran 5 times.

5.2 Scalability Evaluation

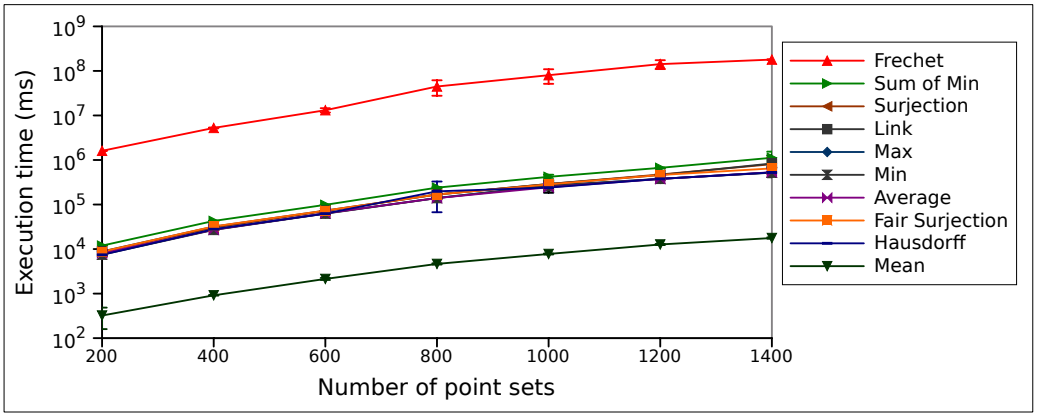


Figure 3: Scalability evaluation on the Nuts dataset.

To quantify how well the measures scale, we measured the runtime of the measures on fragments of growing size of each of the input datasets. This experiment emulates a naive deduplication on datasets of various sizes. The results achieved on Nuts are shown in Figure 3. We chose to show Nuts because it is the smallest and most fine-granular of our datasets. Thus, the measures achieved here represent an upper bound for the runtime behaviour of the different approach. D_{mean} is clearly the most time-efficient approach. This was to be expected as its algorithmic complexity is linear. While most of the other measures are similar in their efficiency, the Fréchet distance sticks out as the slowest to run. Overall, it is at least two orders of magnitude slower than the other measures. These results give a clear answer to question Q_1, which pertains to the time-efficiency of the measures at hand: D_{mean} is clearly the fastest.

5.3 Robustness Evaluation

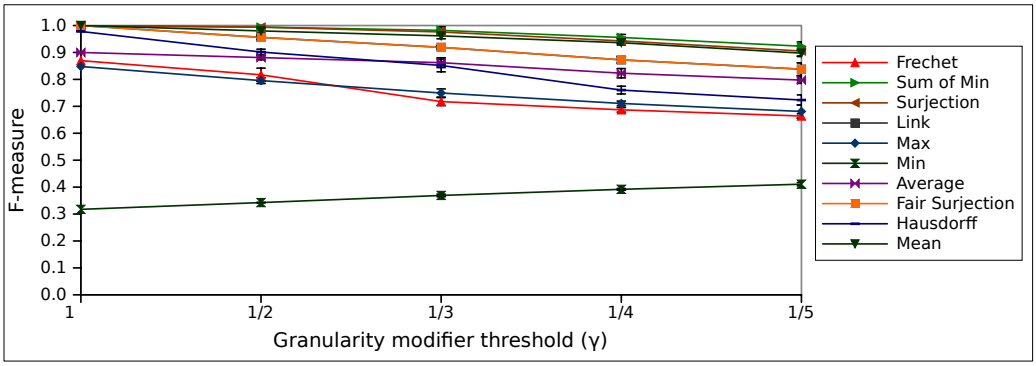
We carried out three types of evaluations to measure the robustness of the measures at hand. First, we measured their robustness against discrepancies in granularity. Then, we measured their robustness against measurement discrepancies. Finally, we combined discrepancies in measurement and granularity and evaluated all our measures against these. We chose to show only a portion of our results for the sake of space. All results can be found at http://limes.sf.net.

5.3.1 Robustness against Discrepancies in Granularity

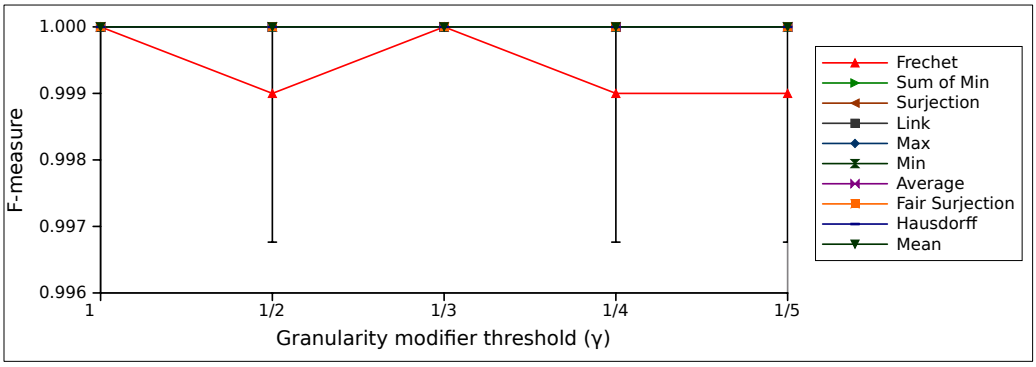
We measured the effect of changes in granularity on the measures at hand by using the five granularity thresholds 1, $\frac{1}{2}$, $\frac{1}{3}$, $\frac{1}{4}$ and $\frac{1}{5}$. Note that the threshold of 1 means that the dataset no change was actually carried out. This setting allows us to answer Q_2, which pertains to the measures that are most adequate for deduplication. On Nuts (see Figure 4(a)), our results suggest that D_{min} is the least robust of the measures w.r.t. the F-measure. In addition to being the least time-efficient measure, Fréchet is also not robust against

changes in granularity. The best performing measure w.r.t. to its F-measure is the *sum of minimums*, followed closely by the surjection and mean measures. On the DBpedia and LGD datasets, all measures apart from the Fréchet distance perform in a similar fashion (see Figure 4(b)). This is yet simply due the sample of the dataset containing point sets that were located far apart from each other. Thus, the answer to question Q_3 on the effect of discrepancies in granularity is that while the *sum of mins* is the least sensitive to changes in granularity, it is closely followed by the sum of mins and the mean measures.

The answer to Q_2 can be derived from the evaluation with the granularity threshold set to 1. Here, mean, fair surjection, surjection, sum of mins and link perform best. Thus, mean should be used because it is more time-efficient.



(a) Nuts

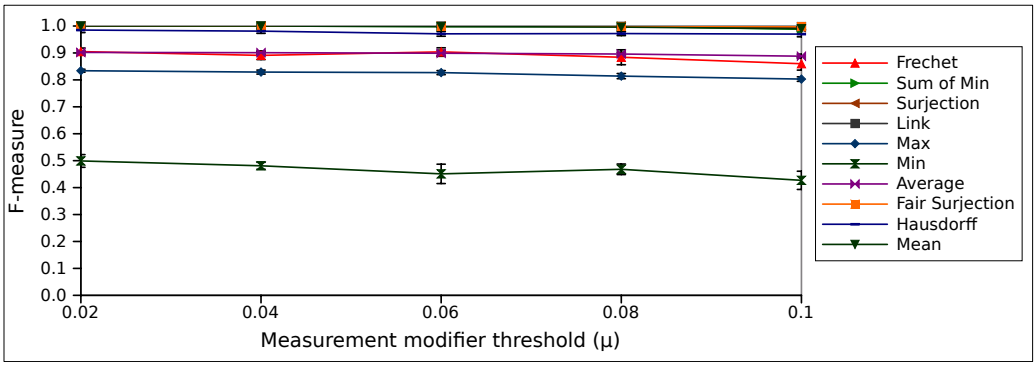


(b) LinkedGeoData

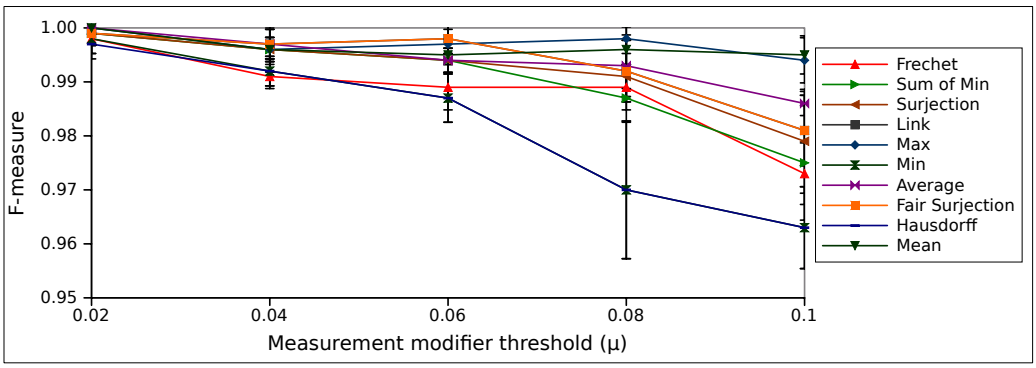
Figure 4: Comparison of different point set distance measures against granularity discrepancies.

5.3.2 Robustness against Measurement Discrepancies

The evaluation of the robustness of the measures at hand against discrepancies in measurement are shown in Figure 5. Interestingly, the results differ across the different datasets. On the Nuts data, where the regions are described with high granularity, five of the measures (mean, fair surjection, link, sum of mins and surjection) perform well. On LGD, the number of points pro resources is considerably smaller. Moreover, the resources are partly far from each other. Here, the Hausdorff distance is the poorest while max and mean perform comparably well. Finally, on the DBpedia dataset, all measures apart from Fréchet are comparable. Our results thus suggest that the answer to Q_4 is as follows: The mean distance is the distance of choice when computing links between geo-spatial datasets which contain measurement errors, especially if the resources described have a high geographical density or the difference in granularity is significant.



(a) Nuts



(b) LinkedGeoData

Figure 5: Comparison of different point set distance measures against measurement discrepancies.

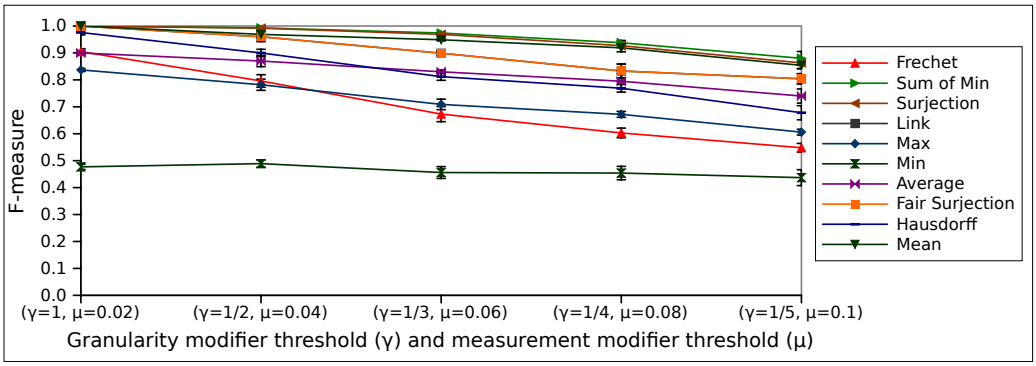
5.3.3 Overall Robustness

We emulated the differences across various real geographic datasets by combining the granularity and the measurement modifiers. Given a dataset S, we generated a modified dataset S' using the granularity modifier. The modified dataset was used as input for a measurement modifier, which generated our final dataset T. The results of our experiments are shown in Figure 6. Again, the results vary across the different datasets. While mean performs well on Nuts 6(a) and LGD, it is surjection that outperforms all the other measures on DBpedia 6(b). This surprising result is due to the measurement errors having only a small effect on our DBpedia sample. Thus, after applying the granularity modifier, the surjection value is rarely affected.

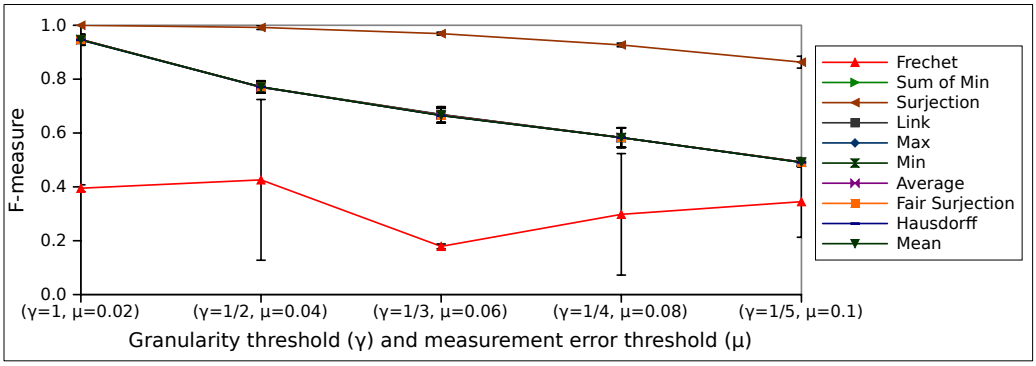
Overall, our results suggest the following answer to Q_5: In most cases, using the mean distance leads to high F-measures. Moreover, mean present the advantage of being an order of magnitude faster than the other approaches. Still, the surjection measure should also be considered when comparing different datasets as it can significantly outperform the mean measure

5.4 Scalability with Orchid

We aimed to know how far the runtime of measures such as mean, surjection and sum of mins can be reduced so as to ensure that these measures can be used on large datasets. We thus combined these measures with the Orchid approach presented in [22]. The idea behind Orchid is to improve the runtime of algorithms for measuring geo-spatial distances by adapting an approach akin to divide-and-conquer. Orchid assumes that it is given a distance measure (not necessarily a metric) m that abides by $m(s,t) \leq \theta \rightarrow \forall s_i \in s\ \exists t_j \in t : \delta(s_i, t_j) \leq \theta$. This condition is obviously not satisfied by all measures considered herein, including min and mean. However,



(a) Nuts



(b) DBpedia

Figure 6: Comparison of different point set distance measures against granularity and measurement discrepancies.

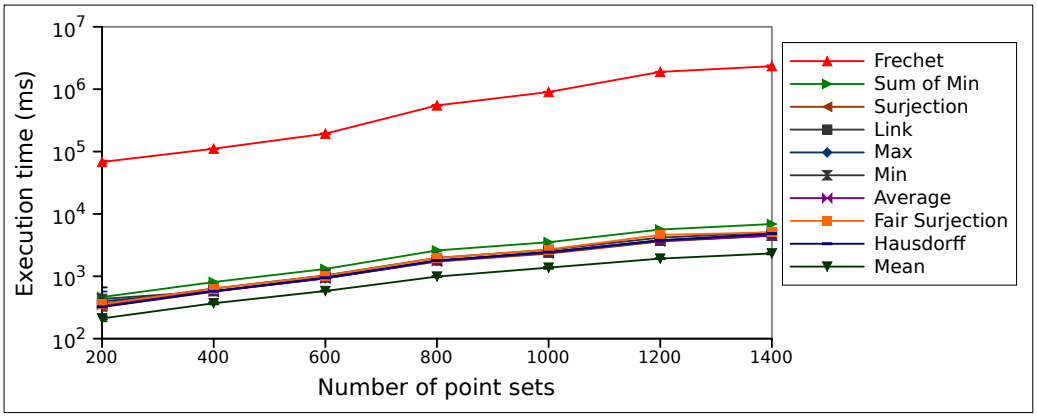
dedicated extensions of Orchid can be developed for these measures. Overall, Orchid begins by partitioning the surface of the planet. The points in a given partition are then only compared with points in partitions that abide by the distance threshold underlying the computation.

We used the default settings of the implementation provided in the LIMES framework and the distance threshold of 0.02 (2.2km). Figure 7(a) shows the runtime results achieved on the same datasets as Figure 3. Clearly, the runtimes of the approaches can be decreased by up to an order of magnitude. Therewith, Orchid allows most measures (i.e., all apart from Fréchet) to scale in a manner comparable to that of the mean measure. Therewith, the measures can now be used on the whole of the datasets at hand. For example, all distance measures apart from the Fréchet distance require less than five minutes to run on the whole of the DBpedia dataset (see 7(b)).

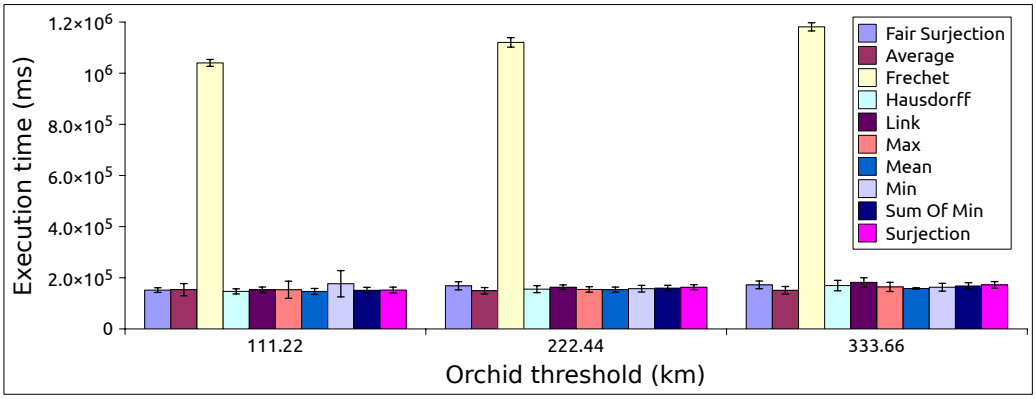
Overall, we can conclude that all measures apart from the Fréchet distance are amenable to being used for link discovery. While *mean performs best overall, surjection-based and minimum-based measures are good candidates* to use if mean returns unsatisfactory results. The Fréchet distance on the other hand seems inadequate for link discovery. This can yet be due to the point set approach chosen in this report. An analysis of the Fréchet distance on the description of resources as polygons remains future work.

5.5 Experiment on Real Datasets

We were interested in knowing whether the mean function performs well on real data. Validating link discovery results on geo-spatial data is difficult due to the lack of reference datasets. We thus measured the increase in



(a) Nuts



(b) DBpedia

Figure 7: Scalability evaluation with ORCHID.

precision and recall achieved by using geo-spatial information by sampling 100 links from the results of real link discovery tasks and evaluating these links manually. The links were evaluated separately by the authors who reached an agreement of 100%.

In the first experiment, we computed links between cities in DBpedia and LinkedGeoData by comparing solely their labels by means of an exact match string similarity. No geo-spatial similarity metric was used, leading to cities being linked if they have exactly the same name. Overall only 74% of the links in our sample were correct. The remaining 26% differed in country or even continent. We can assume that a recall of 1 would be achieved by using this approach as a particular city will most probably have the same name across different geo-spatial datasets. Thus, in the best case, linking geo-spatial resources in DBpedia to LinkedGeoData would only lead to an F-measure of 0.85.

In our second experiment, we extended the specification described above by linking two cities if their names were exact matches (which was used in the first experiment) and the mean distance function between their geometry representation returned a value under 100km. In our sample, we achieved a perfect accuracy and thus an F-measure of 1. While this experiment is small, it clearly demonstrates the importance of using geo-spatial information for linking geo-spatial resources. Moreover, it suggest that the mean distance is indeed reliable on real data. More experiments yet need to be carried out to ensure that the empirical results we got in this experiment are not just a mere artifact in the data. We will achieve this goal by creating a benchmark for geo-spatial link discovery and reporting new results in D3.4.2.

6 Related Work

This report is related to distance measures for point sets and link discovery. Several reviews on distances for point sets have been published. For example, [12] reviews some of the distance functions proposed in the literature presents efficient algorithms for the computation of these measures. [28] presents an approach to compute the similarity between multiple polylines and a polygon using dynamic programming. [3] focuses on the Hausdorff distance and presents an approach for its efficient computation between convex polygons. While the approach is quasi-linear in the number of nodes of the polygons, it cannot deal with non-convex polygons as commonly found in geographic data. [29] present a similar approach that allows approximating Hausdorff distances within a certain error bound, while [6] presents an exact approach. [24] present an approach to compute Hausdorff distances between trajectories using R-trees within an L_2-space. Fréchet distance is basically used in piecewise curve similarity detection like in case of hand writing recognition. For example, [2] introduces an algorithm for computing Fréchet distance between two polygonal curves, while [8] presents a polynomial-time algorithm to compute the homotopic Fréchet distance between two given polygonal curves in the plane avoiding a given set of polygonal obstacles. [10] provides an approximation of Fréchet distance for realistic curves in near linear time.

7 Conclusion

In this report, we presented an evaluation of point set distance measures for link discovery on geo-spatial resources. We evaluated these distances on sample from three different datasets. Our results suggest that while different measures perform best on the data sets we used, the *mean distance measure* is the most time-efficient and overall best measure to use for link discovery. It is thus also the measure to rely upon when the completeness of a dataset is to be measured. Our evaluation also showed that the Fréchet distance is the most sensible to error in location and granularity. This basically means that by computing the Fréchet distance between two resources that are known to describe the same real-world object across different datasets, we can deduce the amount of error contained in the community-driven or the reference dataset. We also showed that all measures apart from the Fréchet distance can scale even on large datasets when combined with an approach such as ORCHID. However, given that Fréchet is only to be used on known equivalent resources, our evaluation suggest that we should be able to compute measures such as completeness, resolution and accuracy even on large datasets such as LinkedGeoData. All the measures presented in this report were integrated in the LIMES framework available at http://limes.sf.net. In future work, we will extend this framework with dedicated versions of ORCHID for the different measures presented herein.

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